

Closed Beam Orbit Calculations in AGS and Fast Beam Extraction

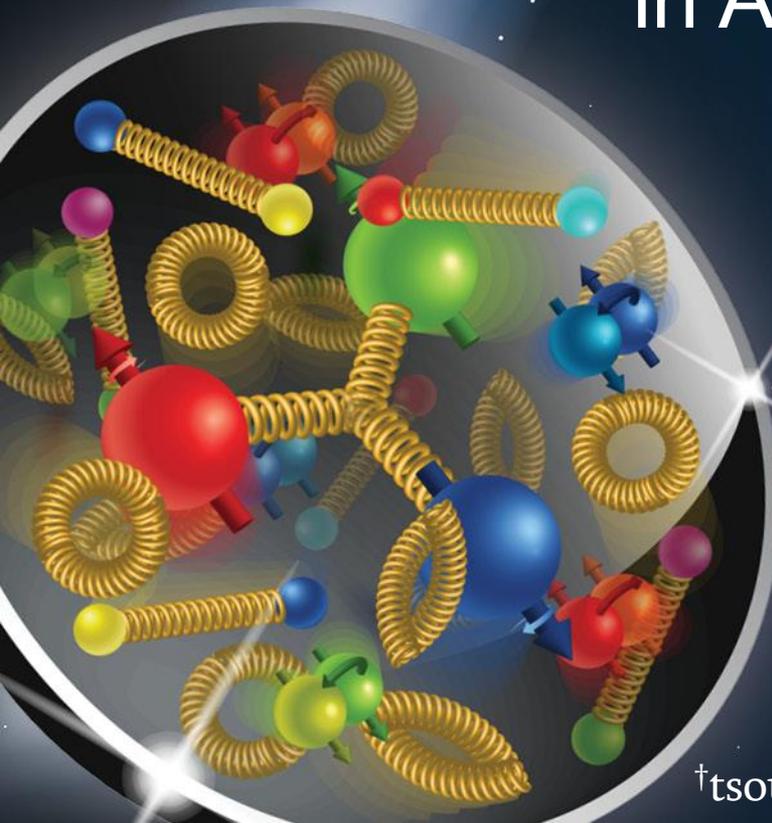
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Brookhaven National Laboratory

S. Machida

STFC Rutherford Appleton Laboratory England

Electron Ion Collider – eRHIC

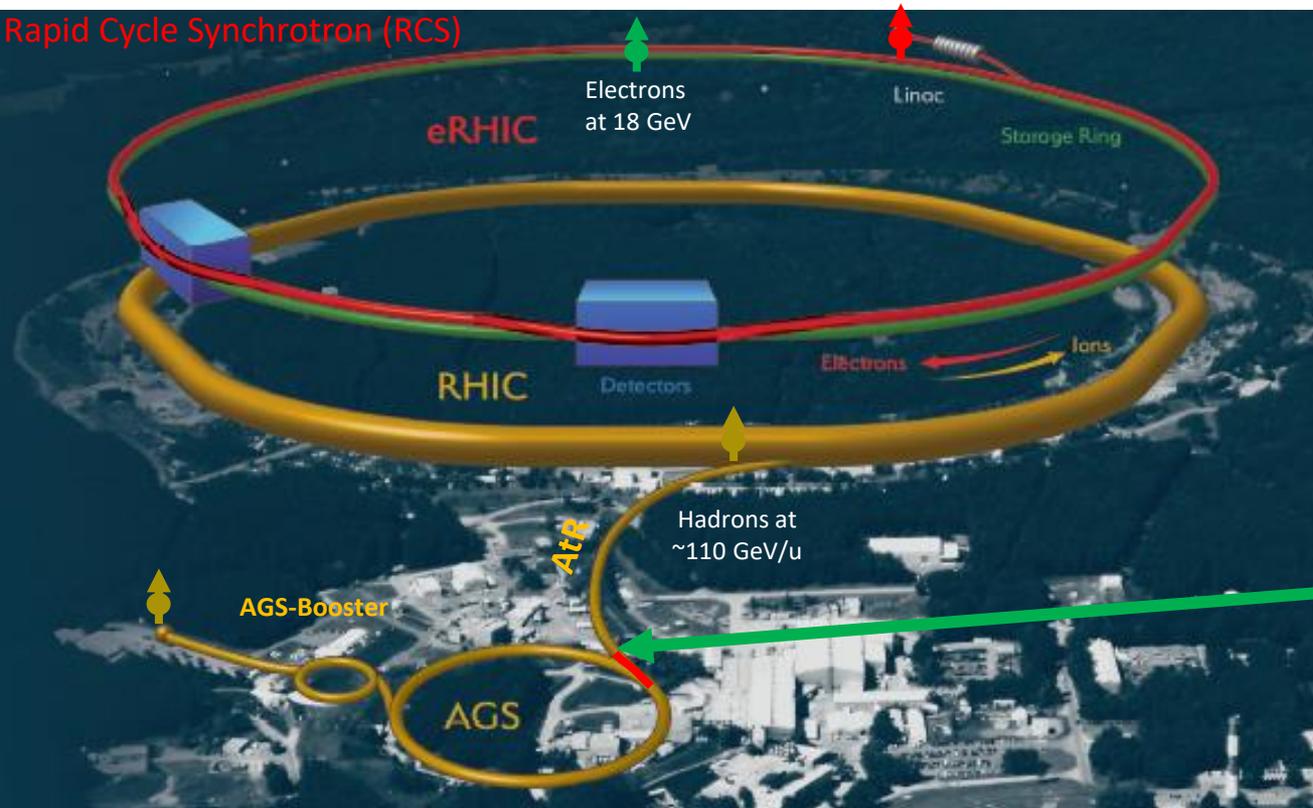
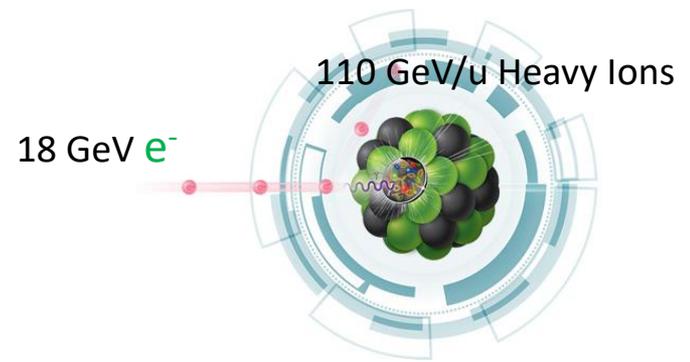


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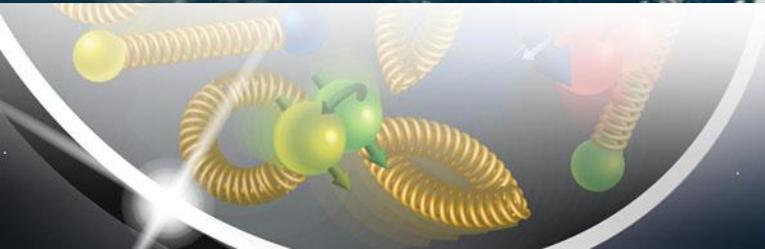
The future eRHIC Collider

Work performed in 1994 published in a BNL internal report
But never reported in a conference.

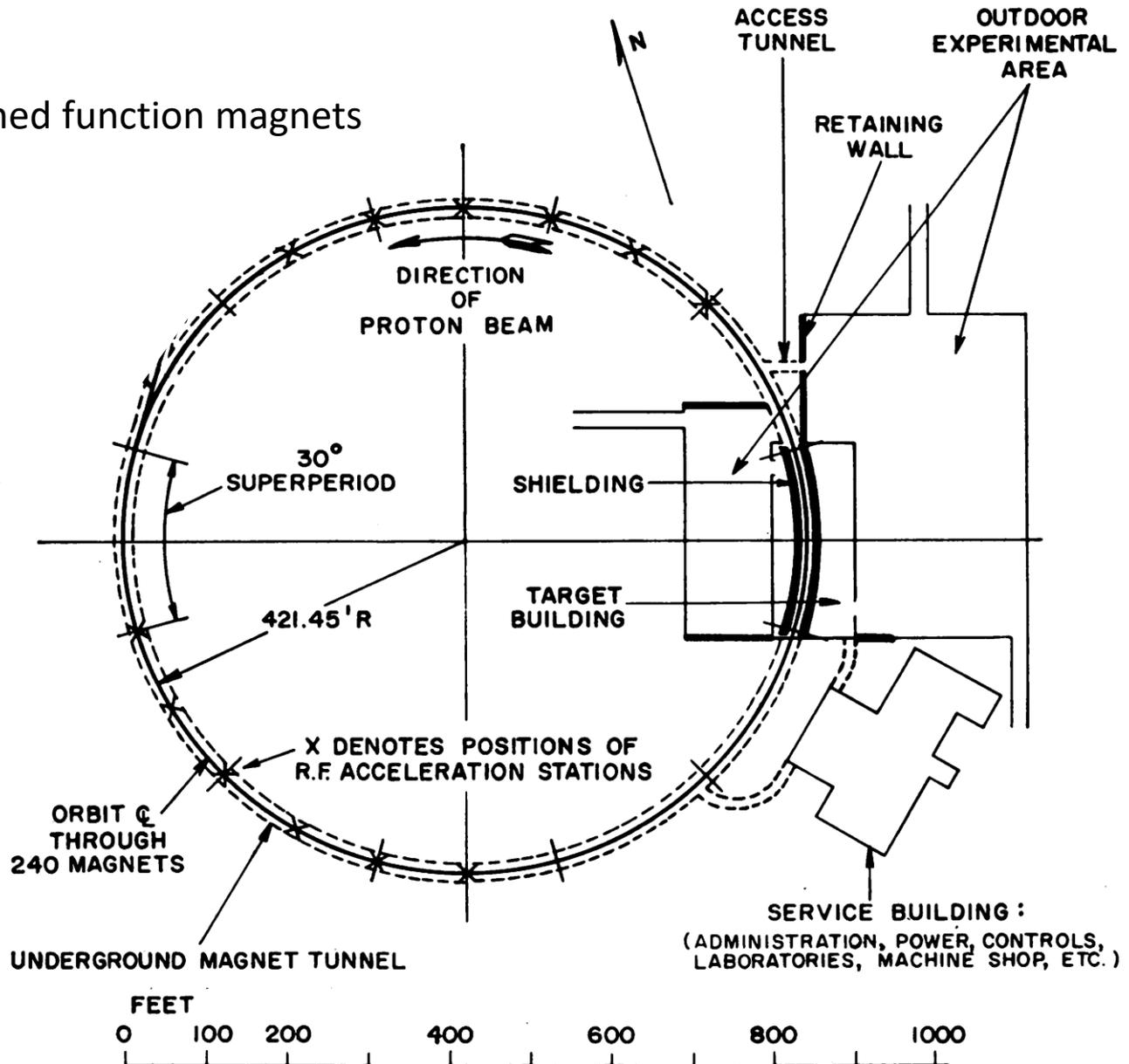


Beam Optics of AGS
based on
measured magnetic fields

Beam parameters at the
Fast Beam Extraction of AGS
or the start of
AGS to RHIC (AtR) line



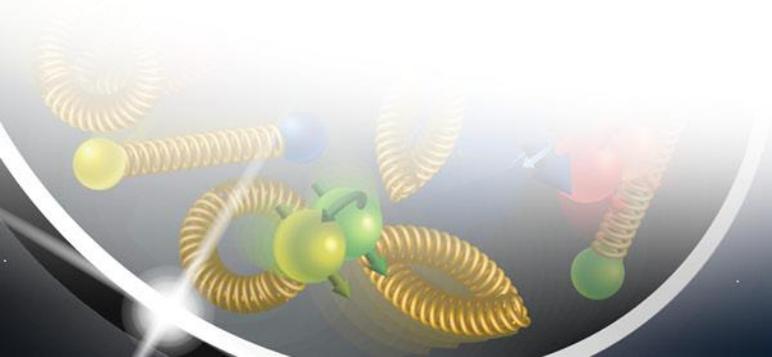
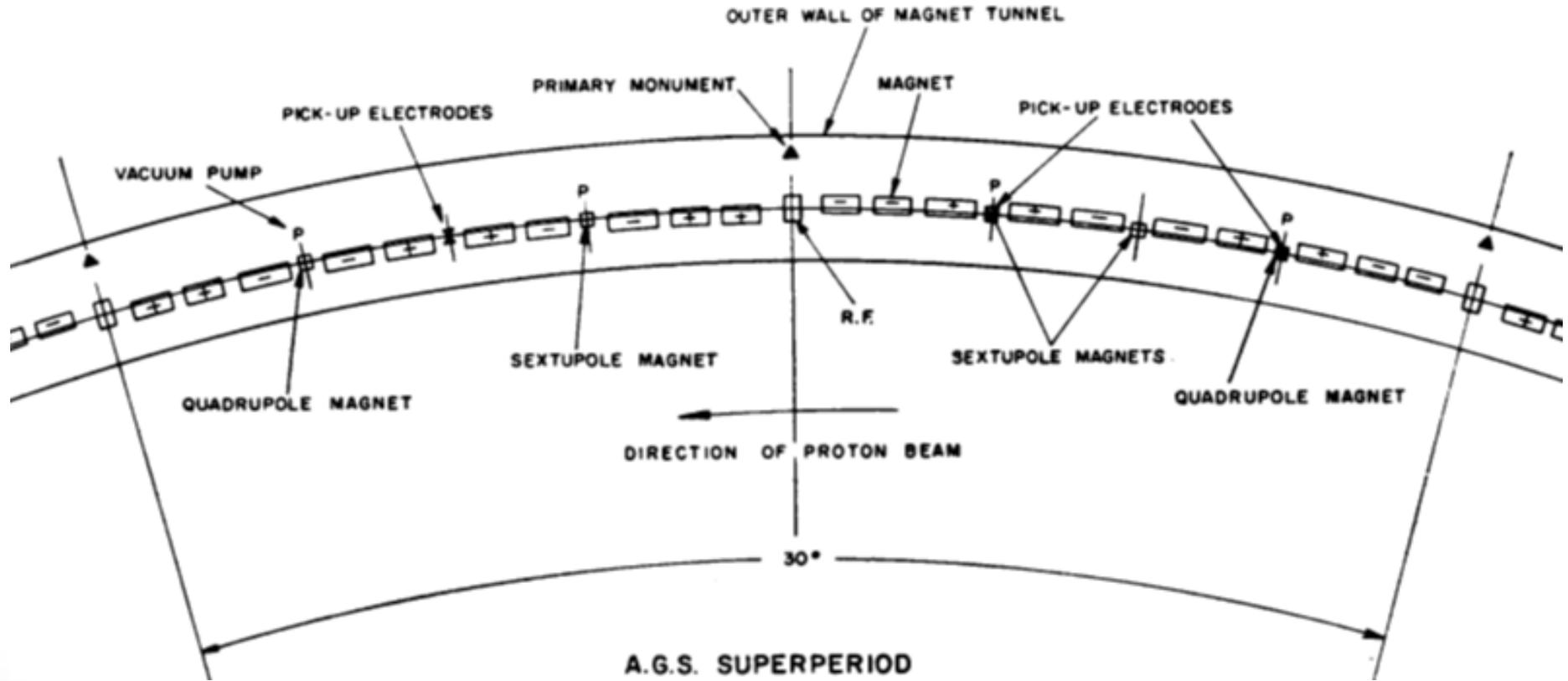
240 Combined function magnets



AGS Superperiod

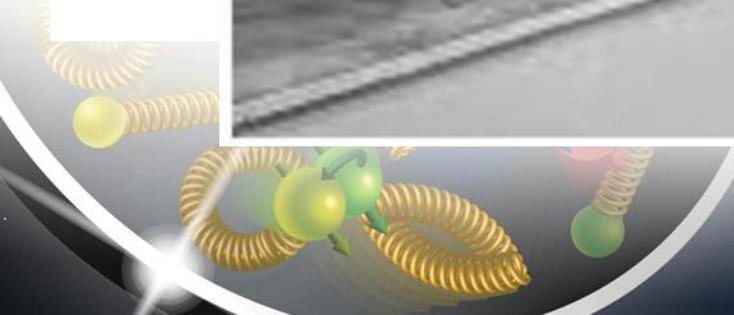
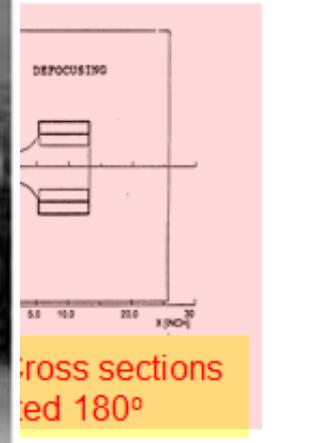
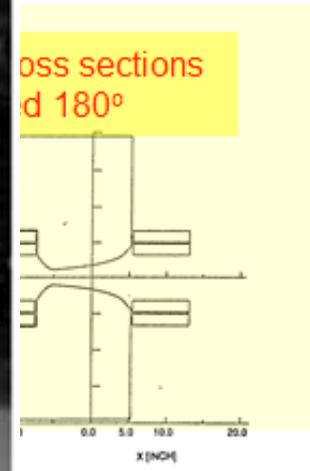
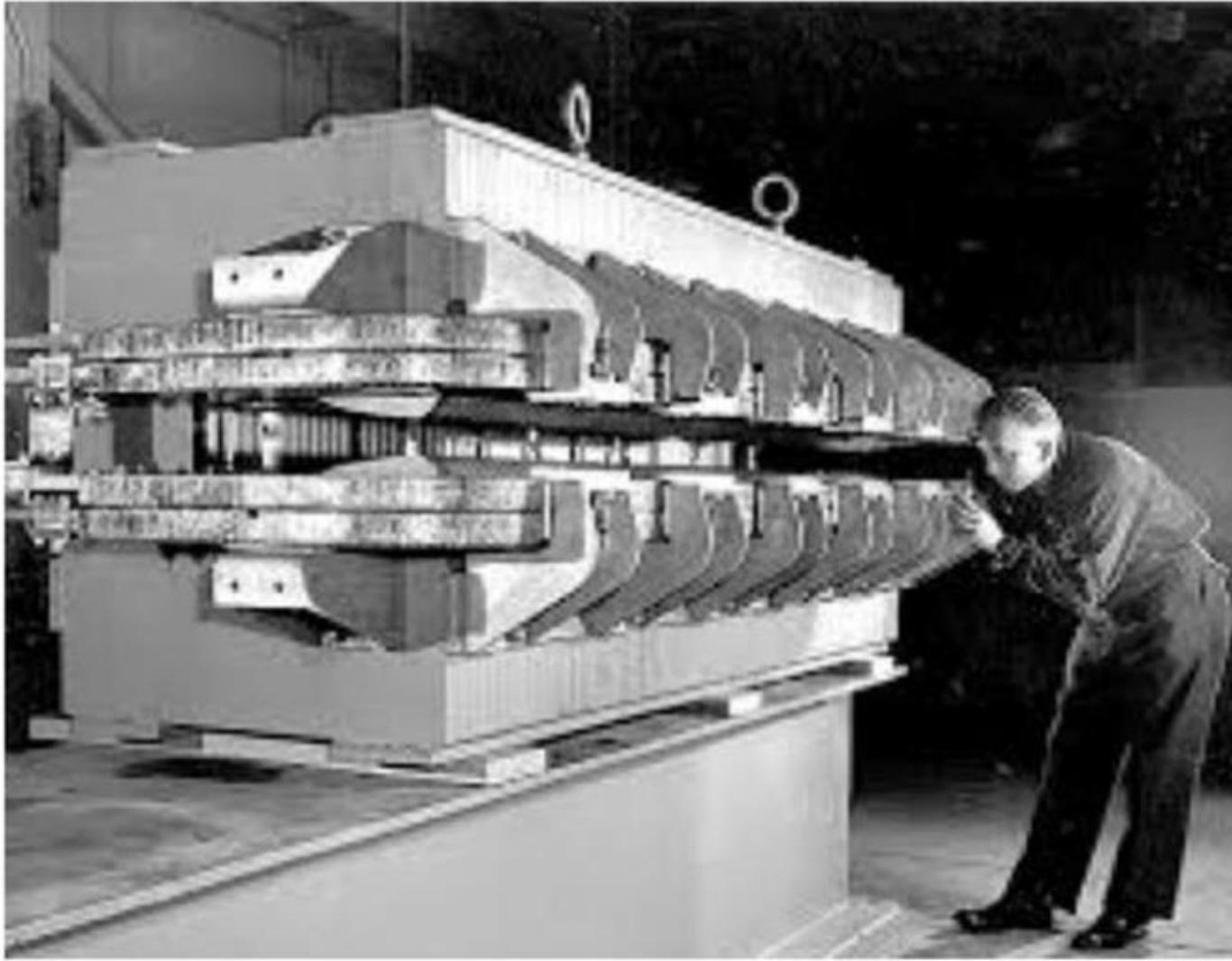
Tune quadrupoles SS03 and SS17

Chromaticity Sextupoles SS05 and SS13

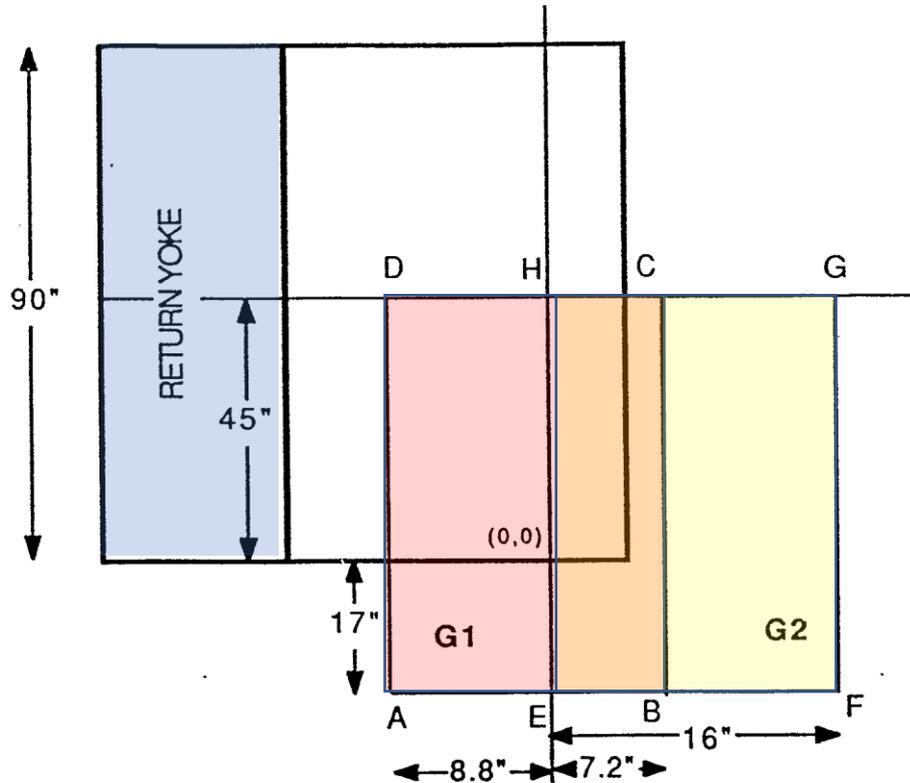


The three types of the ACS Magnets

- | Type |
|------|
| A |
| B |
| C |



The 2D field maps on plane grids

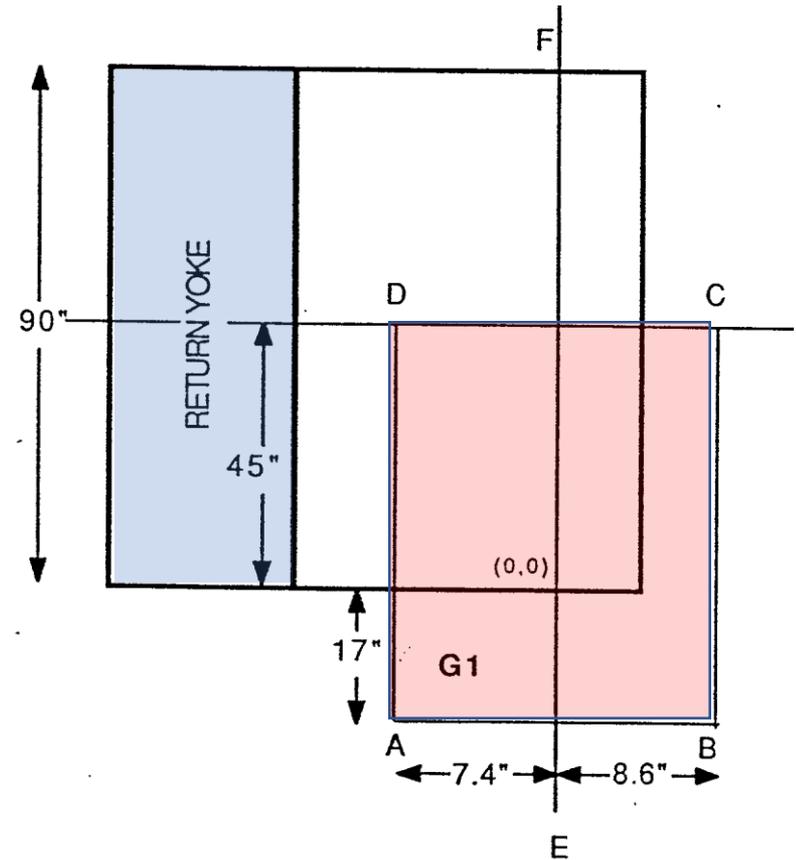


Magnet type A (L=90)

G1 plane $8.8'' \leq x \leq -7.2''$

G2 plane $0.0'' \leq x \leq -16''$

Step in x-transverse 0.10"
Step in z-longitudinal 0.25"



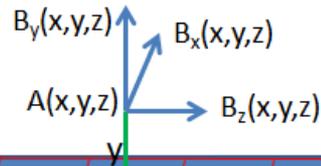
Magnet type C (L=90)

G1 plane $7.4'' \leq x \leq -8.6''$

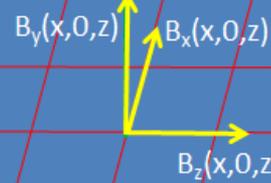
Step in x-transverse 0.10"
Step in z-longitudinal 0.25"

Algorithm to calculate 3D Fields from field maps on a plane

$$B_i(x, y, z) = \sum_{j=0}^4 \frac{1}{j!} \frac{\partial^j B_i(x, y, z)}{\partial y^j} \Big|_{y=0} y^j = \sum_{j=0}^4 a_{ij}(x, z) y^j \quad (1)$$

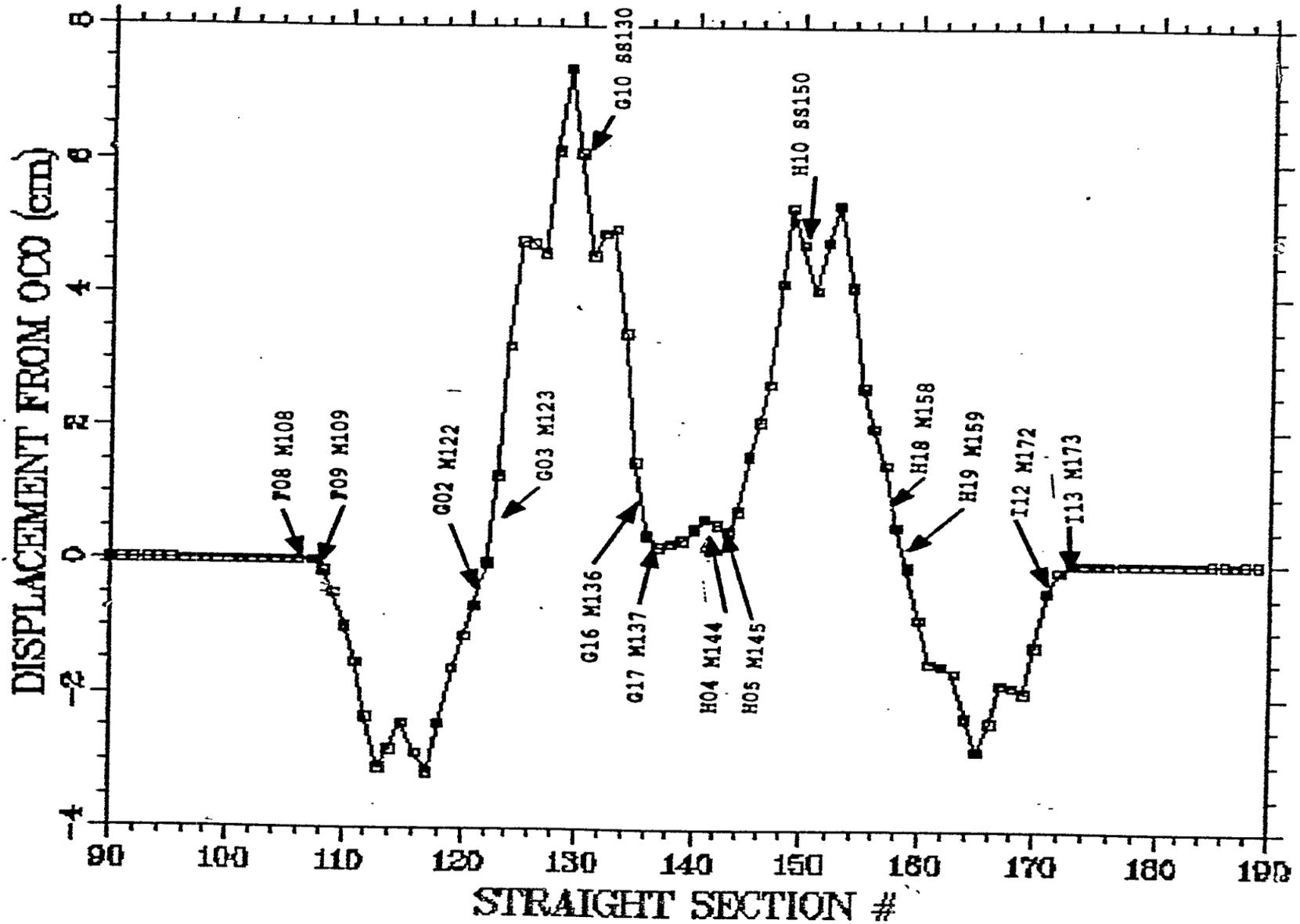


$$\vec{\nabla} \cdot \vec{B}(x, y, z) = 0 \quad \text{and} \quad \vec{\nabla} \times \vec{B}(x, y, z) = 0$$

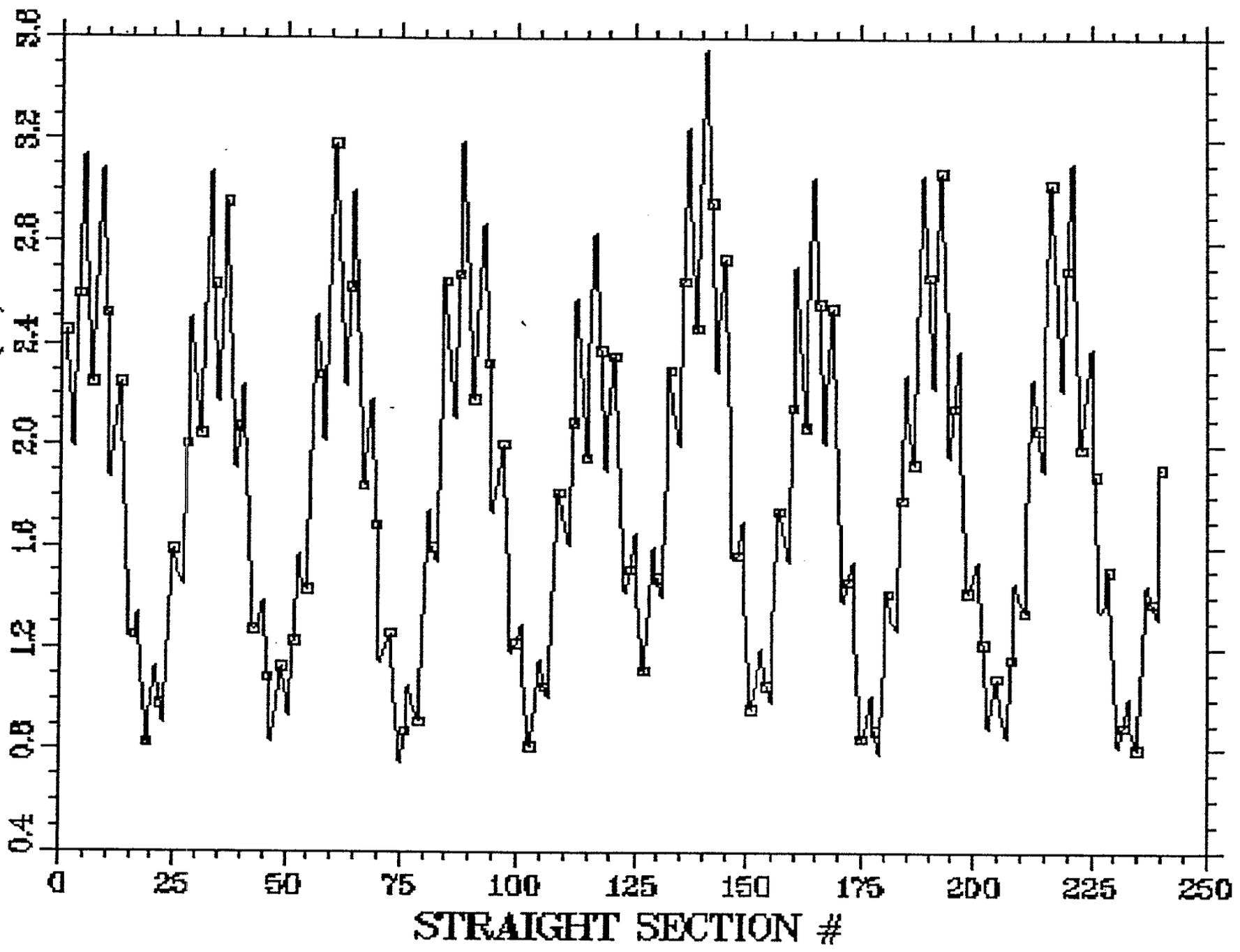


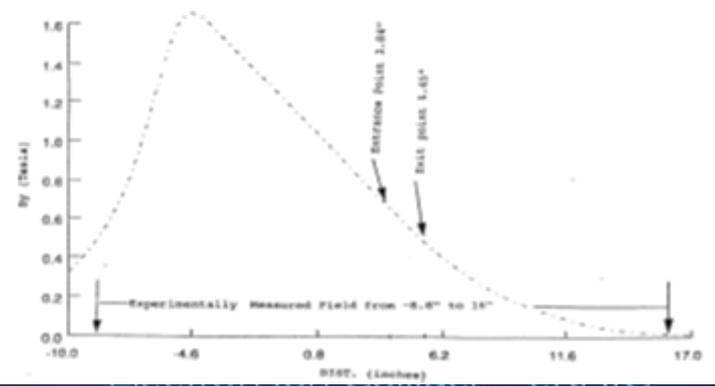
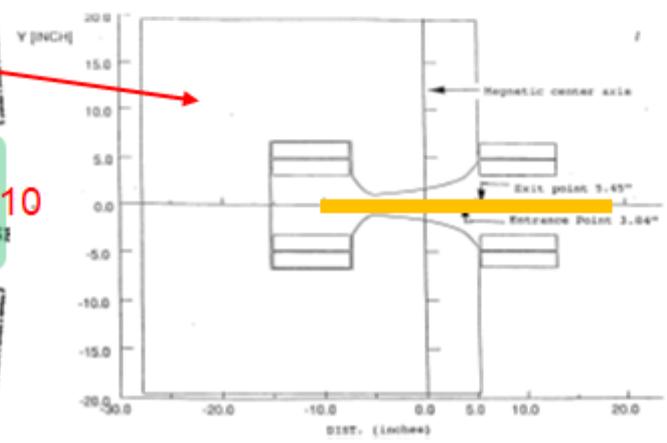
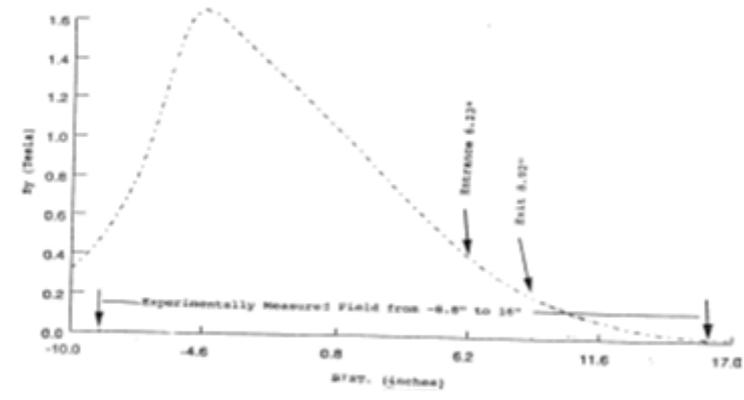
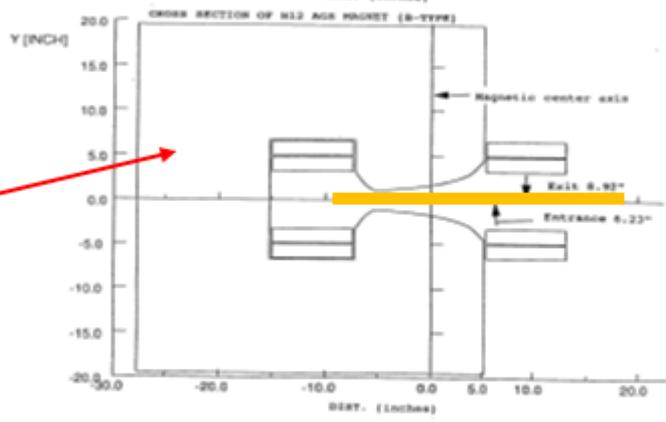
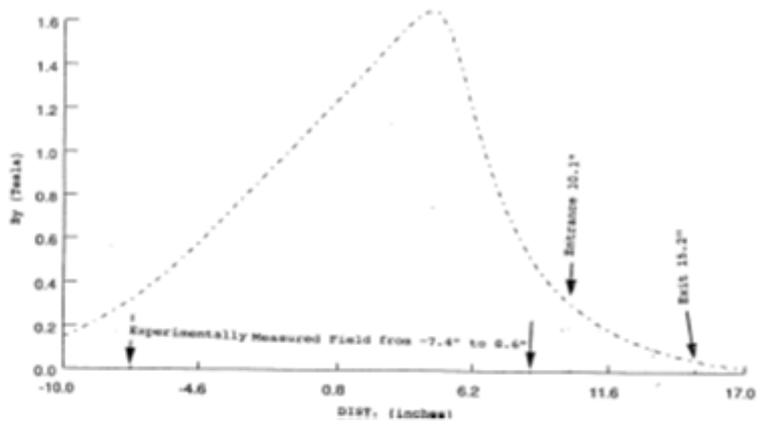
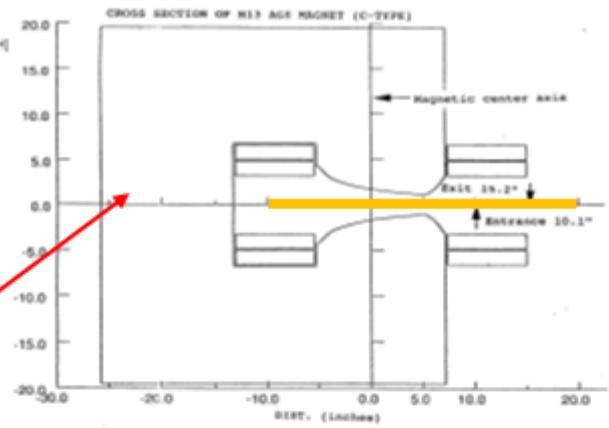
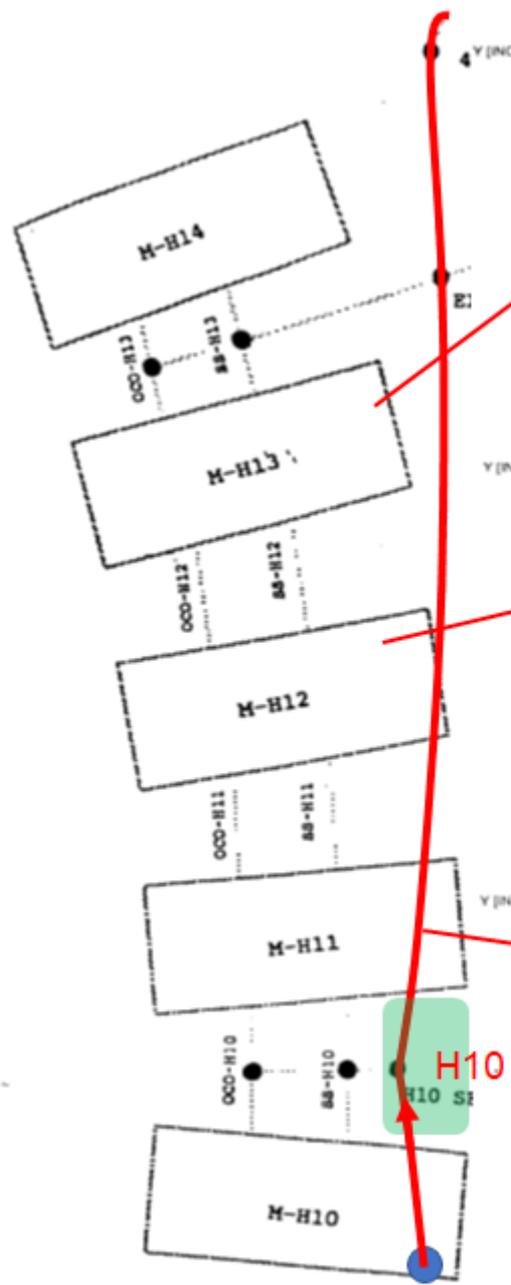
The coefficients α_{ij} are expressed in terms of the measure field components on the plane and their derivatives with respect to x, z .

The Extraction Beam bumps G10 and H10



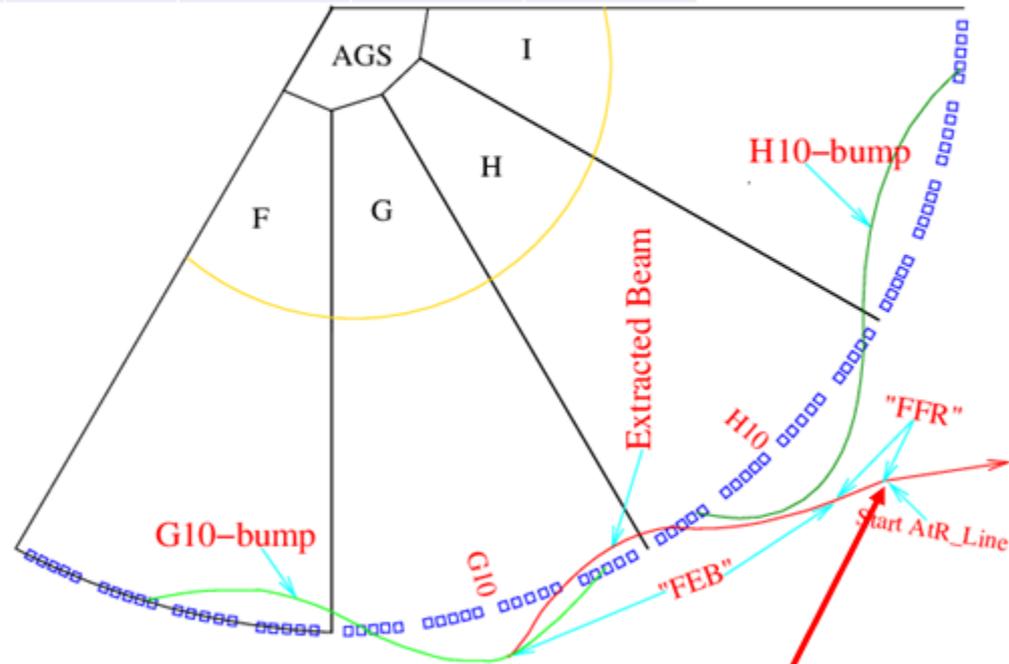
DISPERSION (m)





R Matrix G10-kicker to Start-AtR					
-1.8261	-17.443	0.0	0.0	0.0	-2.5889
0.17912	1.1634	0.0	0.0	0.0	0.2517
0.0	0.0	1.125	-15.016	0.0	0.0
0.0	0.0	0.186	-1.5855	0.0	0.0
-0.0041	1.3785	0.0	0.0	1	0.0
0.0	0.0	0.0	0.0	0.0	1.0

	H13
β_x	34.7 [m]
α_x	-3.4
η_x	-1.06 [m]
η'_x	-0.68
β_x	8.1 [m]
α_x	1.06



$$\begin{pmatrix} R_{11}^2 & -2R_{11}R_{12} & R_{12}^2 \\ -R_{11}R_{21} & R_{12}R_{21} + R_{11}R_{22} & -R_{12}R_{22} \\ R_{21}^2 & -2R_{21}R_{22} & R_{22}^2 \end{pmatrix} \begin{pmatrix} \beta \\ \alpha \\ \gamma \end{pmatrix}_{start} = \begin{pmatrix} \beta \\ \alpha \\ \gamma \end{pmatrix}_{end}$$

Thank you for your attention

