

Zgoubi

Recent Developments and Future Plans

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Future Plans for Zgoubi Include Enhancements to both Performance and Usability

Implement a Zgoubi graphical interface in Sirepo.

Implement single-click execution of Zgoubi on available linux clusters.

GUI

Update the Zgoubi code base to the Fortran 2018.

Re-implement Zgoubi's particle update algorithm.

performance

Parallelize Zgoubi using Fortran 2018, including coarrays.

Implement symplectic tracking for field maps.

capabilities

Add closed-orbit correction to Zgoubi.

Assess and improve the spin dynamics in electron and ion rings for the eRHIC design.

science

Benchmark Zgoubi with BMad and other codes used for simulating JLEIC ring designs.





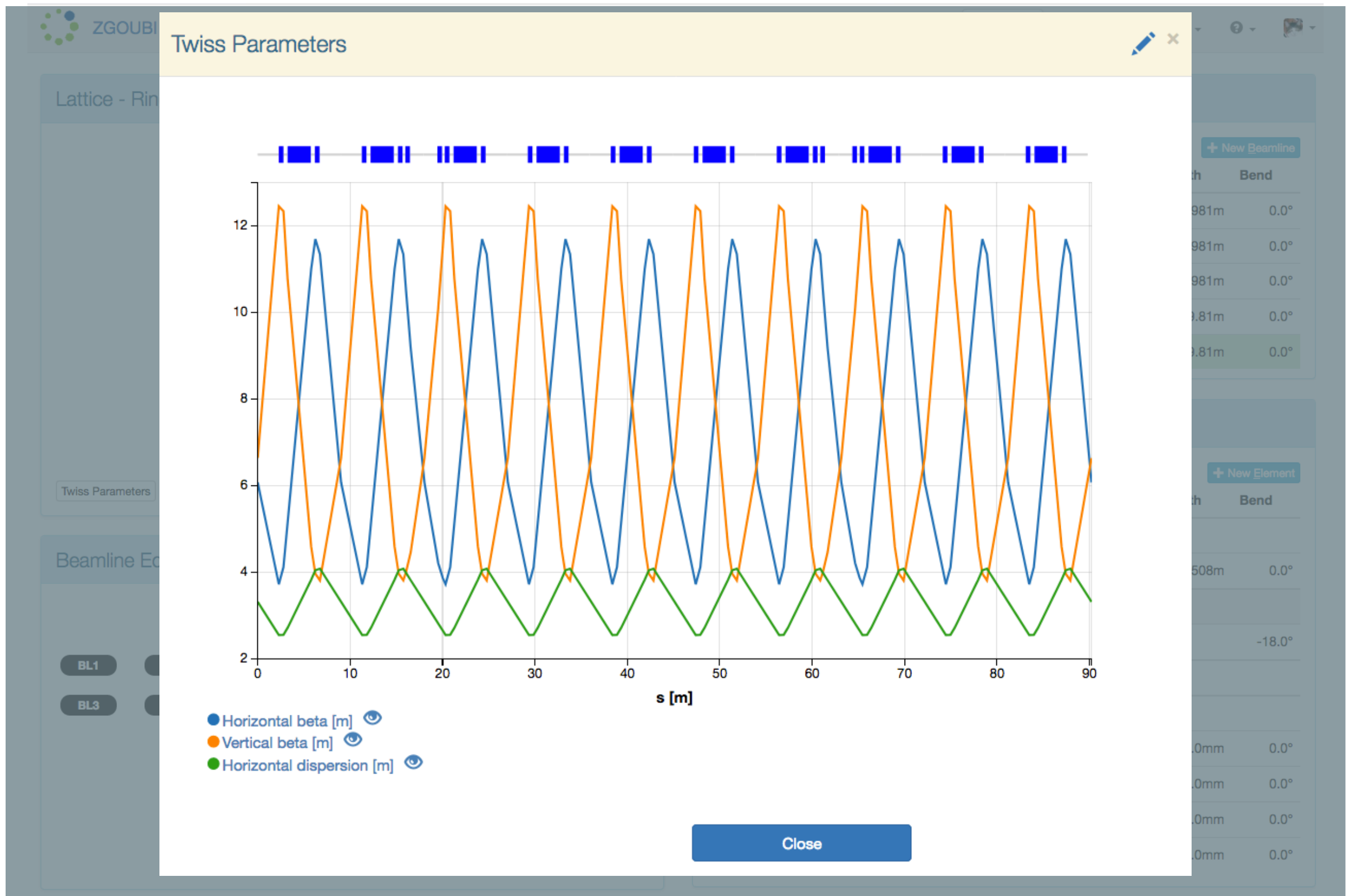




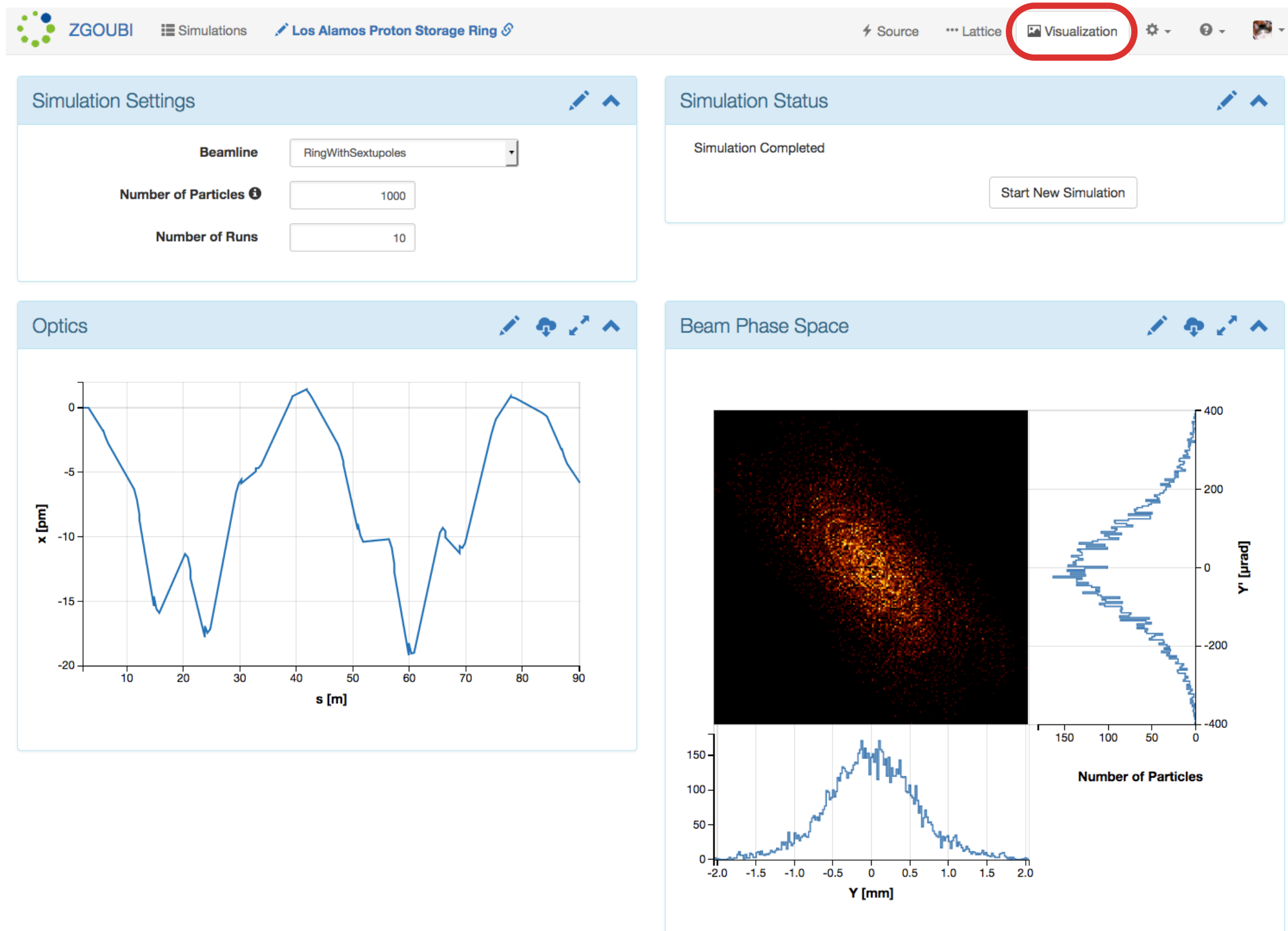




Streamline Zgoubi Simulations: Implement a Sirepo Interface for Zgoubi—cont.



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Improve Performance:

Re-implement the Zgoubi Particle Update

Lorentz force law: $\frac{d\vec{p}}{dt} = q(\vec{E} + \vec{v} \times \vec{B})$

Zgoubi tracks normalized velocity: $\vec{u} = \frac{1}{v}\vec{v}$ $\vec{p} = m\gamma\vec{v} = q(B\rho)\vec{u}$

Then Zgoubi writes the Lorentz force law in the form

$$\frac{d}{ds}(B\rho)\vec{u} = (B\rho)'\vec{u} + (B\rho)\vec{u}' = \frac{1}{v}\vec{E} + \vec{u} \times \vec{B}$$

$$\implies (B\rho)', \vec{u}', (B\rho)'', \vec{u}'', (B\rho)^{(3)}, \vec{u}^{(3)}, \dots$$

... and the particle update in the form

$$\vec{r}^f \approx \vec{r} + \Delta s \vec{u} + \frac{\Delta s^2}{2!} \vec{u}' + \dots + \frac{\Delta s^6}{6!} \vec{u}^{(5)}$$

$$\vec{u}^f \approx \vec{u} + \Delta s \vec{u}' + \frac{\Delta s^2}{2!} \vec{u}'' + \dots + \frac{\Delta s^5}{5!} \vec{u}^{(5)}$$

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$$\frac{d}{ds}(B\rho)\vec{u} = (B\rho)'\vec{u} + (B\rho)\vec{u}' = \frac{1}{v}\vec{E} + \vec{u} \times \vec{B}$$

distance along trajectory

$$\implies (B\rho)', \vec{u}', (B\rho)'', \vec{u}'', (B\rho)^{(3)}, \vec{u}^{(3)}, \dots$$

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Improve Performance:

Re-implement the Zgoubi Particle Update—cont.

If *no* electric field, then $\vec{u}' = \vec{u} \times \vec{b}$, where $\vec{b} = \frac{1}{B\rho} \vec{B}$.

Successive derivatives of $\vec{u}$ are computed as

$$\vec{u}'' = \vec{u}' \times \vec{b} + \vec{u} \times \vec{b}', \quad \vec{u}''' = \vec{u}'' \times \vec{b} + 2\vec{u}' \times \vec{b}' + \vec{u} \times \vec{b}'', \quad \dots$$

Successive derivatives of $\vec{b}$ are computed as

$$\vec{b}' = \sum_i \frac{\partial \vec{b}}{\partial x_i} u_i$$

$$\vec{b}'' = \sum_i \frac{\partial \vec{b}}{\partial x_i} u'_i + \sum_{ij} \frac{\partial^2 \vec{b}}{\partial x_i \partial x_j} u_i u_j$$

$\vdots$

Improve Performance: Re-implement the Zgoubi Particle Update—cont.

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$\vdots$

Truncated power series algebras (TPSAs) perform essentially the same computations; hence we can take advantage of efficient TPSA algorithms. Doing so reduces both memory footprint and corresponding arithmetic by roughly a factor of 3.

Improve Performance:

Parallelize Zgoubi using Fortran 2018

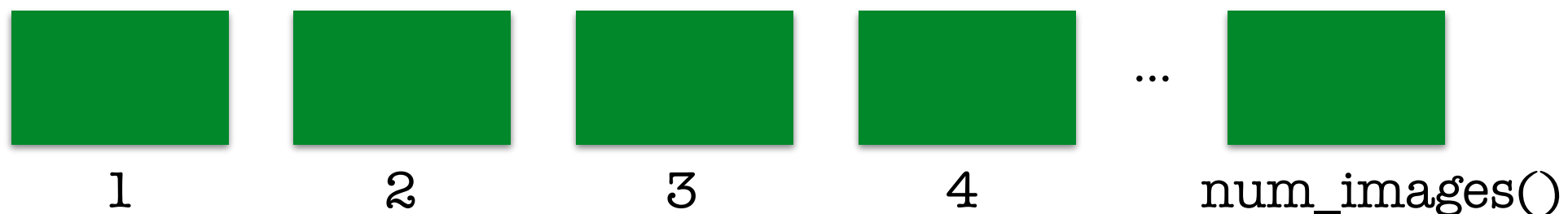
The coarray programming model is designed to answer the question ‘What is the smallest change required to convert Fortran into a robust and efficient parallel language?’.

— John Reid, *ISO/IEC JTC1/SC22/WG5 N1824* (2010)

Coarray syntax implements a Single Program Multiple Data (SPMD) model.

A single program is replicated in units called *images*.

The number of images may be chosen at compile time.



```
real :: a[*] ! scalar coarray
real, dimension(10) :: x[*], y[*] ! array coarray
real :: m(0:21,6)[*] ! matrix coarray
type(particle) :: ptcl(128)[*] ! derived type coarray
real :: array(10,20)[10,-1:8,0:*] ! more complex coarray
```

```
x(:) = y(:)[q] ! access remote data on image q
```

Improve Performance:

Parallelize Zgoubi using Fortran 2018

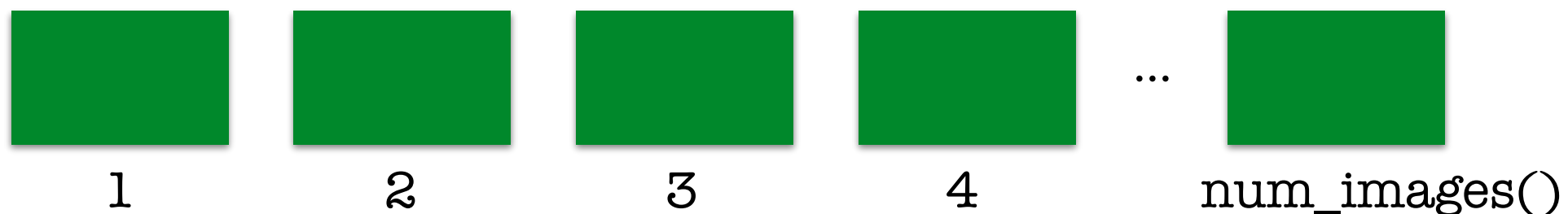
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A coindex indicates communication.

The programmer must ensure that

- * coarray indices are properly resolved,
- * synchronization occurs as appropriate.

The new Fortran standard includes new intrinsics that simplify the process.

Improve Performance:

Parallelize Zgoubi using Fortran 2018—cont.

Opportunities for parallellizing Zgoubi:

Distribute particles on multiple processors.

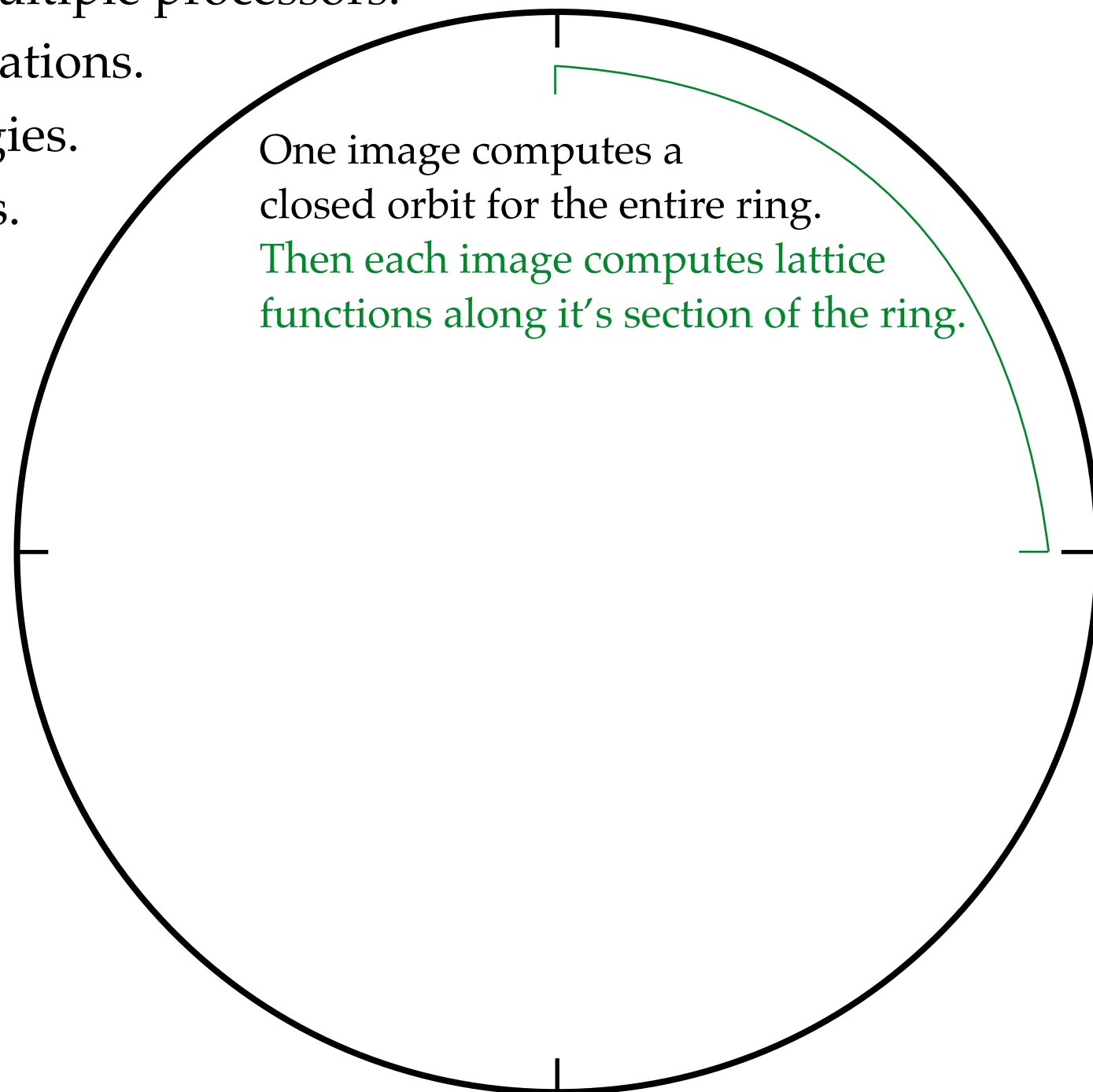
Distribute lattice computations.

Distribute machine energies.

Distribute misalignments.

Various scans:

dynamic aperture;
polarization studies
etc.



Thank you!

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